Idris Exercises: Part 2

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Questions

1. Implement the following function, which states that if you add the same value onto the front of equal lists, the resulting lists are also equal:

   ```idris
   same_cons : {xs : List a} -> {ys : List a} ->
   xs = ys -> x :: xs = x :: ys
   ```

   Since this function represents an equality proof, it is sufficient to know that your definition type checks.

2. Define a type `ThreeEq` which expresses that three values must be equal.
   
   (Hint: `ThreeEq` should have the type `a -> b -> c -> Type`)

3. Implement the following function:

   ```idris
   allSameS : (x, y, z : Nat) -> ThreeEq x y z -> ThreeEq (S x) (S y) (S z)
   ```

4. Implement the following function which checks whether two lists are equal and returns a proof if so:

   ```idris
   checkEqList : DecEq a => (xs : List a) -> (ys : List a) -> Maybe (xs = ys)
   ```

   Can you improve the definition using `Dec` instead of `Maybe`?

5. The following definition of a reverse function on vectors doesn’t type check:

   ```idris
   my_reverse : Vect n elem -> Vect n elem
   my_reverse [] = []
   my_reverse (x :: xs) = my_reverse xs ++ [x]
   ```

   How can you correct it using `rewrite`?
   
   (Hint: Look up the library function `plusCommutative`)

6. The following definition of a reverse function is more efficient, but incomplete:

   ```idris
   my_reverse : Vect n a -> Vect n a
   my_reverse xs = reverse' [] xs
   where reverse' : Vect n a -> Vect m a -> Vect (n+m) a
       reverse' acc [] = ?reverseProof_nil acc
       reverse' acc (x :: xs)
           = ?reverseProof_xs (reverse' (x::acc) xs)
   ```

   Complete this definition by implementing the holes `reverseProof_nil` and `reverseProof_xs`.